

**2022A7****IMAGINARY NUMBERS****ANSWERS**

**Level 1:** Here are the answer in order with some explanations given:

a)  $2 * 3i = 6i$

a. We can separate the 3 from the  $i$ , so that the equation becomes  $2 * 3 * i$ .  $2 * 3$  is 6, and  $6 * i$  is  $6i$ .

b)  $3 + 4i = 3 + 4i$

a. This cannot be reduced any farther, so the given equation is the final answer!

c)  $(6 + i) * 2 + 3i = (12 + 2i) + 3i = 12 + 5i$

a. Imaginary numbers do not affect the order of operations, so we can multiply what's inside the parenthesis by two to start our solution.

d)  $(6i)^2 = -36$

a. We can distribute the square to the equation so that we get  $6^2 * i^2$ . Solving these, we get  $36 * -1$ , and then our answer:  $-36$ .



Imaginary numbers help a lot with calculations for AC power which is what our turbines deliver to industrial customers.

**Level 2:** Here are the answer in order with some explanations given:

- a)  $(4.5 + 6i) * 2i = -12 + 9i$   
a. Just like we mentioned in part c of the Level 1 questions, imaginary numbers do not affect the order of operations.
- b)  $3i * (99 + 4) = 309i$
- c)  $5.6i * 7.5i = -42$   
a. Decimals do not affect how we multiply imaginary numbers.
- d)  $12i - 8i = 4i$   
a. Subtraction works the same way too!
- e)  $i^3 = -i$   
a. Let's split up this problem.  $i^3 = i * i * i = i^2 * i$ . Great! We know  $i^2 = -1$ , so now we have  $-1 * i$  or  $-i$ .

In future Wind Studies, we'll use these imaginary numbers to talk about impedance, phase angles in polar and exponential form, and power calculations with leading and lagging currents!